

2.2

$$(e) (a + b + c')(a'b' + c) = aa'b' + ac + ba'b' + bc + c'a'b' + c'c = ac + bc + a'b'c'$$

$$(f) a'b'c + ab'c + abc + a'bc = b'c + bc = c$$

2.4

$$(d) (A' + C)(A' + C')(A + B + C'D) = (A' + CC')(A + B + C'D)$$

$$= A'(A + B + C'D) = AA' + A'B + A'C'D = A'(B + C'D)$$

$$(e) A'BD' + ABC'D' + ABCD' = BD'(A' + AC' + AC)$$

$$= BD'$$

2.9

$$(c) F' = [z + z'(v'w + xy)]' = z'[z'(v'w + xy)]'$$

$$= z'[z'v'w + xyz']' = z'[(z'v'w)'(xyz')']$$

$$= z'[(z + v + w') + (x' + y' + z)]$$

$$= z'z + z'v + z'w' + z'x' + z'y' + z'z$$

$$= z'(v + w' + x' + y')$$

2.11

$$(b) F = ac + bc' = abc + ab'c + abc' + a'bc'$$

$$F(a, b, c) = \Sigma(2, 5, 6, 7)$$

a b c F

0 0 0 0

0 0 1 0

0 1 0 1

0 1 1 0

1 0 0 0

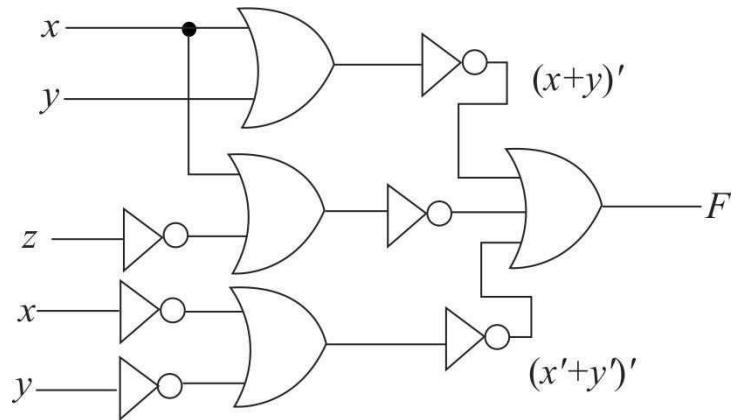
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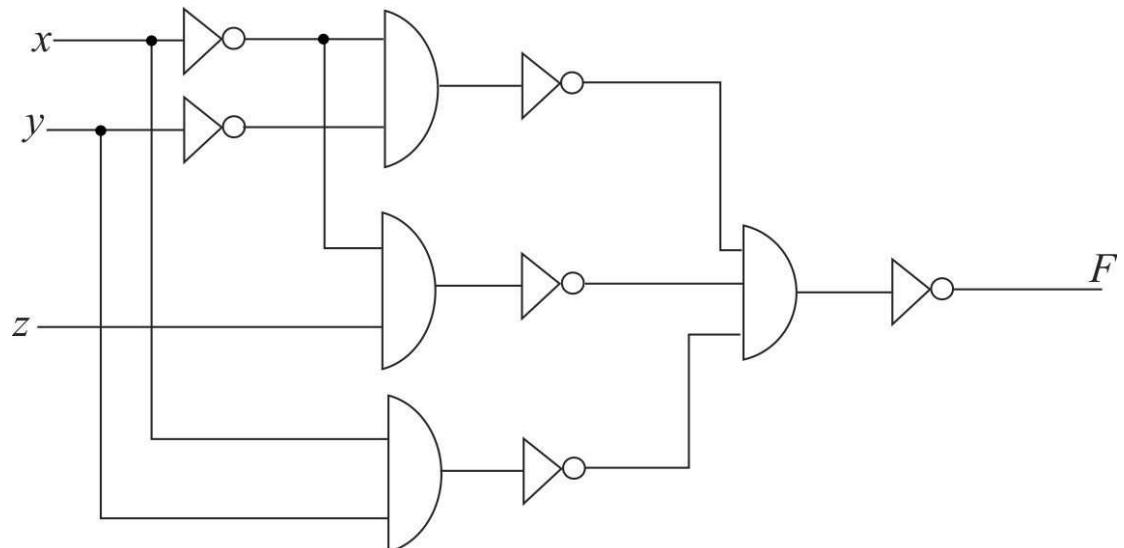
1 1 1 1

2.14

$$(b) F = xy' + xz + xy = (x+y)' + (x+z)' + (x'+y)'$$



$$(c) F = x'y' + x'z + xy = [(x'y')'(x'z)'(xy)']'$$



2.22

$$(b) x' + z(x+y')(y+z') = x' + (xz + zy')(y+z') = x' + xyz$$

$\Rightarrow x' + yz \rightarrow SOP\ form$

$\Rightarrow (x' + y)(x' + z) \rightarrow POS\ form$

2.28 (a) $y = a(bcd)'e = a(b' + c' + d')e$

$$y = a(b' + c' + d')e = ab' + ac' + ad' \\ = \Sigma(17, 19, 21, 23, 25, 27, 29)$$

| a bcde | y | a bcde | y |
|--------|---|--------|---|
| 0 0000 | 0 | 1 0000 | 0 |
| 0 0001 | 0 | 1 0001 | 1 |
| 0 0010 | 0 | 1 0010 | 0 |
| 0 0011 | 0 | 1 0011 | 1 |
| 0 0100 | 0 | 1 0100 | 0 |
| 0 0101 | 0 | 1 0101 | 1 |
| 0 0110 | 0 | 1 0110 | 0 |
| 0 0111 | 0 | 1 0111 | 1 |
| | 0 | | 0 |
| 0 1000 | 0 | 1 1000 | 0 |
| 0 1001 | 0 | 1 1001 | 1 |
| 0 1010 | 0 | 1 1010 | 0 |
| 0 1011 | 0 | 1 1011 | 1 |
| 0 1100 | 0 | 1 1100 | 0 |
| 0 1101 | 0 | 1 1101 | 1 |
| 0 1110 | 0 | 1 1110 | 0 |
| 0 1111 | 0 | 1 1111 | 0 |

(b) $y_1 = a \oplus (c + d + e) = a'(c + d + e) + a(c'd'e') = a'c + a'd + a'e + ac'd'e'$

$$y_2 = b'(c + d + e)f = b'cf + b'df + b'ef$$

$$y_1 = a(c + d + e) = a'(c + d + e) + a(c'd'e') = a'c + a'd + a'e + ac'd'e'$$

$$y_2 = b'(c + d + e)f = b'cf + b'df + b'ef$$

| $a'-c---$ | $a'--d--$ | $a'---e-$ | $a-c'd'e'$ | $-b' c--f$ | $-b' -d-f$ | $-b' --ef$ |
|-------------|-------------|-------------|-------------|-------------|-------------|------------|
| 001000 = 8 | 000100 = 8 | 000010 = 2 | 100000 = 32 | | | |
| 001001 = 9 | 000101 = 9 | 000011 = 3 | 100001 = 33 | | | |
| 001010 = 10 | 000110 = 10 | 000110 = 6 | 110000 = 34 | | | |
| 001011 = 11 | 000111 = 11 | 000111 = 7 | 110001 = 35 | | | |
| 001100 = 12 | 001100 = 12 | 001010 = 10 | | | | |
| 001101 = 13 | 001101 = 13 | 001011 = 11 | | | | |
| 001110 = 14 | 001110 = 14 | 001110 = 14 | | | | |
| 001111 = 15 | 001111 = 15 | 001111 = 15 | | | | |
| 011000 = 24 | 010100 = 20 | 010010 = 18 | 001001 = 9 | 001001 = 9 | 000011 = 3 | |
| 011001 = 25 | 010101 = 21 | 010011 = 19 | 001011 = 11 | 001011 = 11 | 000111 = 7 | |
| 011010 = 26 | 010110 = 22 | 010110 = 22 | 001101 = 13 | 001101 = 13 | 001011 = 11 | |
| 011011 = 27 | 010111 = 23 | 010111 = 23 | 001111 = 15 | 001111 = 15 | 001111 = 15 | |
| 011100 = 28 | 011100 = 28 | 011010 = 26 | 101001 = 41 | 101001 = 41 | 100011 = 35 | |
| 011101 = 29 | 011101 = 29 | 011001 = 27 | 101011 = 43 | 101011 = 43 | 100111 = 39 | |
| 011110 = 30 | 011110 = 30 | 011110 = 30 | 101101 = 45 | 101101 = 45 | 101011 = 51 | |
| 011111 = 31 | 011111 = 31 | 011111 = 31 | 101111 = 47 | 101111 = 47 | 101111 = 55 | |

$$y_1 = \Sigma (2, 3, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 18, 19, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35)$$

$$y_2 = \Sigma (3, 7, 9, 13, 15, 35, 39, 41, 43, 45, 47, 51, 55)$$

| <i>ab cdef</i> | <i>y₁ y₂</i> |
|----------------|------------------------------------|----------------|------------------------------------|----------------|------------------------------------|----------------|------------------------------------|
| 00 0000 | 0 0 | 01 0000 | 0 0 | 10 0000 | 1 0 | 11 0000 | 0 0 |
| 00 0001 | 0 0 | 01 0001 | 0 0 | 10 0001 | 1 0 | 11 0001 | 0 0 |
| 00 0010 | 1 0 | 01 0010 | 1 0 | 10 0010 | 1 0 | 11 0010 | 0 0 |
| 00 0011 | 1 1 | 01 0011 | 1 0 | 10 0011 | 1 1 | 11 0011 | 0 1 |
| 00 0100 | 0 0 | 01 0100 | 0 0 | 10 0100 | 0 0 | 11 0100 | 0 0 |
| 00 0101 | 0 0 | 01 0101 | 0 0 | 10 0101 | 0 0 | 11 0101 | 0 0 |
| 00 0110 | 1 0 | 01 0110 | 1 0 | 10 0110 | 0 0 | 11 0110 | 0 0 |
| 00 0111 | 1 1 | 01 0111 | 1 0 | 10 0111 | 0 1 | 11 0111 | 0 1 |
| 00 1000 | 1 0 | 01 1000 | 1 0 | 10 1000 | 0 0 | 11 1000 | 0 0 |
| 00 1001 | 1 1 | 01 1001 | 1 0 | 10 1001 | 0 1 | 11 1001 | 0 0 |
| 00 1010 | 1 0 | 01 1010 | 1 0 | 10 1010 | 0 0 | 11 1010 | 0 0 |
| 00 1011 | 1 0 | 01 1011 | 1 0 | 10 1011 | 0 1 | 11 1011 | 0 0 |
| 00 1100 | 1 0 | 01 1100 | 1 0 | 10 1100 | 0 0 | 11 1100 | 0 0 |
| 00 1101 | 1 1 | 01 1101 | 1 0 | 10 1101 | 0 1 | 11 1101 | 0 0 |
| 00 1110 | 1 0 | 01 1110 | 1 0 | 10 1110 | 0 0 | 11 1110 | 0 0 |
| 00 1111 | 1 1 | 01 1111 | 1 0 | 10 1111 | 0 1 | 11 1111 | 0 0 |